# Structure of Dierbium Decavanadate 25-Hydrate, $\mathrm{Er}_{2} \mathbf{V}_{10} \mathbf{O}_{28} \mathbf{2 5} \mathbf{H}_{\mathbf{2}} \mathrm{O}$ 

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#### Abstract

M_{r}=1741 \cdot 52\), triclinic, $P \overline{1}, a=9.168$ (9), $b=10.002$ (15), $c=12.703$ (6) $\AA, \quad \alpha=68.87$ (8), $\beta$ $=77.52(8), \quad \gamma=89.34(10)^{\circ}, \quad V=1058 \AA^{3}, \quad Z=1$, $D_{m}=2.66, \quad D_{x}=2.73 \mathrm{Mg} \mathrm{m}^{-3}, \quad$ Мо $K \alpha, \quad \lambda=$ $0.71069 \AA, \mu=5.88 \mathrm{~mm}^{-1}, F(000)=840$, room temperature, $R=4.8 \%, R_{w}=5.7 \%$ for 3639 independent reflections with $I>4 \sigma(I)$. The unit cell contains one $\left(\mathrm{V}_{10} \mathrm{O}_{28}\right)^{6-}$ anion located on a symmetry center, two symmetry-related $\left[\mathrm{Er}\left(\mathrm{H}_{2} \mathrm{O}\right)_{8}{ }^{3+}\right.$ cations and nine interstitial water molecules, one with its O at a symmetry center. The structure forms layers of both decavanadate polyanions and rare-earth polyhedra (which do not share coordination O atoms), and layers of water molecules of hydration. These layers are parallel to (001) and are held together by hydrogen bonding.


Introduction. As part of a general study of the crystal chemistry of the rare-earth decavanadates (Rigotti, Punte, Rivero, Escobar \& Baran, 1981, and references therein), we have solved the structure of $\mathrm{Er}_{2} \mathrm{~V}_{10} \mathrm{O}_{28} .25 \mathrm{H}_{2} \mathrm{O}$, which is isostructural with $\mathrm{Ln}_{2}-$ $\mathrm{V}_{10} \mathrm{O}_{28} \cdot 25 \mathrm{H}_{2} \mathrm{O}(\mathrm{Ln}=\mathrm{Eu}, \mathrm{Gd}, \mathrm{Tb}$, Dy and Ho$)$.

Experimental. Bright-orange crystalline plates of the hydrated rare-earth decavanadates grown and kindly supplied by Dr E. J. Baran and co-workers, Area de Quimica Inorgánica, UNLP, Argentina; syntheses have been described by Rigotti et al. (1981). Density measured pycnometrically. Crystal of irregular shape, $0.4 \times 0.4 \times 0.2 \mathrm{~mm}$. Enraf-Nonius CAD-4 diffractometer, graphite-monochromatized Mo $K \alpha$ radiation, $\omega / \theta$ scan mode. Lattice parameters obtained from high $2 \theta$ values ( $17-30^{\circ}$ ) of 25 reflections. Scan width $(1+0.34 \tan \theta)^{\circ}$, aperture $(1.4+0.8 \tan \theta) \mathrm{mm}$, maximum scan time 60 s , range explored 3.0 to $50.0^{\circ}$ in $2 \theta$. Three reflections ( 603,654 and $7 \overline{3} \overline{5}$ ) monitored every 100 reflections showed an overall $\sigma$ (relative instability) of 0.02 .3639 unique reflections $[I>4 \sigma(I)]$

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from a total of $7385, R_{\text {int }}=0.022$. Lp correction, absorption and extinction ignored. Heavy-atom method (SHELX, Sheldrick, 1976). All remaining (nonhydrogen) atoms from $\Delta F$ synthesis. Anisotropic blocked diagonal matrix and $F$ magnitudes. $f$ curves from Cromer \& Mann (1968) for $\mathrm{Er}^{3+}, \mathrm{V}^{5+}$ and $\mathrm{O}^{-}$ (for the decavanadate ion). Refinement with about 12 data per independent parameter, final $R=0.048$, $R_{w}=0.057 ; \quad w=16 \cdot 6 /\left[\sigma^{2}(F)+0.0008 F^{2}\right] . \quad(\Delta / \sigma)_{\max }$ $0 \cdot 14 ;(\Delta / \sigma)_{\text {ave }} 0.003$. Max. and min. height in final $\Delta \rho$ map 2.99 and $-4.94 \mathrm{e}^{\AA^{-3}}$.

Discussion. Final atomic coordinates are in Table 1. $\ddagger$
The decavanadate polyanion $\mathrm{V}_{10} \mathrm{O}_{28}^{6-}$ is formed by a highly condensed system of $\mathrm{VO}_{6}$ octahedra, shown in Fig. 1 , as previously described for $\mathrm{K}_{2} \mathrm{Zn}_{2} \mathrm{~V}_{10} \mathrm{O}_{28}$.$16 \mathrm{H}_{2} \mathrm{O}$ (Evans, 1966), $\mathrm{Ca}_{3} \mathrm{~V}_{10} \mathrm{O}_{28} .17 \mathrm{H}_{2} \mathrm{O}$ (Swallow, Ahmed \& Barnes, 1966), $\mathrm{Na}_{6} \mathrm{~V}_{10} \mathrm{O}_{28} \cdot 18 \mathrm{H}_{2} \mathrm{O}$ (Durif, Averbuch-Pouchot \& Guitel, 1980), $\mathrm{Y}_{2} \mathrm{~V}_{10} \mathrm{O}_{28} .24 \mathrm{H}_{2} \mathrm{O}$, $\mathrm{La}_{2} \mathrm{~V}_{10} \mathrm{O}_{28} \cdot 20 \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{Nd}_{2} \mathrm{~V}_{10} \mathrm{O}_{28} \cdot 28 \mathrm{H}_{2} \mathrm{O}$ (Saf'yanov, $\mathrm{Kuz}{ }^{\prime} \min$ \& Belov, 1979) and [ $\mathrm{NHC}_{7} \mathrm{H}_{9} \mathrm{l}_{4}\left[\mathrm{~V}_{10} \mathrm{H}_{2} \mathrm{O}_{28}\right]$ (Debaerdemaeker, Arrieta \& Amigo, 1982).

Table 2 shows the interatomic distances and angles of the three types of $\mathrm{VO}_{6}$ octahedra (Evans, 1966). Regarding the geometry of the decavanadate polyanion, two types of distortions can be discussed.
(a) Distortions of $\mathrm{VO}_{6}$ octahedra, which do not significantly affect the intrinsic mmm orthorhombic symmetry of the polyanion. The severe distortions in the $\mathrm{VO}_{6}$ octahedra - displacement of $\mathrm{V}_{\mathrm{III}}$-type atoms towards one edge of the octahedra and displacement of $\mathrm{V}_{\mathrm{I}}$ and $\mathrm{V}_{\mathrm{II}}$ towards one apex - are mainly due to internal Coulombic repulsion (Evans, 1966). These distortions can be interpreted on the grounds put forward by Baur (1970) and Brown \& Shannon (1973). The empirical bond-strength-bond-length curves for

[^1]oxides proposed by the latter authors are very useful in accounting for bonding in highly distorted environments, since the concepts of ionic radius and coordination number are avoided. The correlation between distortion (mean-square relative deviation of bond length from the average) and average $\mathrm{V}-\mathrm{O}$ bond length within each $\mathrm{VO}_{6}$ octahedron in erbium decavanadate is similar to that given in Fig. 7 of Brown \& Shannon (1973).

Table 1. Fractional positional parameters and equivalent isotropic thermal parameters with e.s.d.'s in parentheses

|  | $x$ | $y$ | $z$ | $U_{\text {eq }}{ }^{*}\left(\AA^{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| $V(1)$ | 0.0068 (1) | 0.2162 (1) | 0.6123 (1) | 0.026 |
| $V(2)$ | 0.9141 (1) | 0.3547 (1) | 0.3784 (1) | 0.029 |
| $V(3)$ | 0.9328 (1) | 0.3532 (1) | 0.7971 (1) | 0.033 |
| V (4) | 0.8232 (1) | 0.4913 (1) | 0.5717 (1) | 0.022 |
| $V(5)$ | 0.2595 (1) | 0.3697 (1) | 0.6641 (1) | 0.030 |
| $\mathrm{O}(1)$ | 0.9741 (5) | 0.0622 (4) | 0.6039 (4) | 0.043 |
| $\mathrm{O}(2)$ | 0.9028 (5) | 0.1946 (4) | 0.7573 (4) | 0.036 |
| $\mathrm{O}(3)$ | 0.1925 (5) | 0.2064 (4) | 0.6430 (4) | 0.037 |
| $\mathrm{O}(4)$ | 0.8317 (4) | 0.3137 (4) | 0.5490 (3) | 0.023 |
| $\mathrm{O}(5)$ | 0.0981 (4) | 0.3222 (4) | 0.4420 (3) | 0.027 |
| $\mathrm{O}(6)$ | 0.0389 (4) | 0.4393 (4) | 0.6004 (3) | 0.026 |
| $\mathrm{O}(7)$ | 0.8822 (5) | 0.1971 (5) | 0.3771 (4) | 0.054 |
| $\mathrm{O}(8)$ | 0.7413 (4) | 0.4400 (4) | 0.3498 (4) | 0.031 |
| $\mathrm{O}(9)$ | 0.0290 (5) | 0.4491 (4) | 0.2359 (4) | 0.050 |
| O(10) | 0.8377 (5) | 0.2982 (5) | 0.9298 (4) | 0.054 |
| $\mathrm{O}(11)$ | 0.1246 (5) | 0.3147 (4) | 0.8062 (4) | 0.042 |
| $\mathrm{O}(12)$ | 0.7575 (5) | 0.4263 (4) | 0.7162 (4) | 0.041 |
| $\mathrm{O}(13)$ | 0.3213 (4) | 0.4464 (4) | 0.4880 (3) | 0.033 |
| O(14) | 0.4169 (5) | 0.3259 (5) | 0.6962 (4) | 0.048 |
| Er | 0.4601 (1) | 0.1303 (1) | 0.2600 (1) | 0.031 |
| OW(15) | 0.2860 (5) | 0.0690 (5) | 0.1678 (4) | 0.055 |
| OW (16) | 0.5037 (5) | 0.2824 (5) | 0.3589 (4) | 0.070 |
| $\mathrm{OW}(17)$ | 0.5935 (5) | 0.0317 (5) | 0.1234 (4) | 0.056 |
| $\mathrm{O} W(18)$ | 0.6644 (6) | 0.0397 (5) | 0.3400 (4) | 0.066 |
| OW(19) | 0.2477 (5) | 0.1107 (5) | 0.4011 (4) | 0.058 |
| OW (20) | 0.3397 (6) | 0.3412 (5) | 0.1706 (4) | 0.069 |
| $\mathrm{O} W(21)$ | 0.5978 (5) | $0 \cdot 1206$ (5) | 0.6415 (4) | 0.060 |
| OW(22) | 0.6444 (6) | 0.3056 (5) | 0.1280 (5) | 0.084 |
| OW(23) | 0.5358 (6) | 0.2032 (5) | 0.8962 (4) | 0.067 |
| OW(24) | 0.1086 (6) | 0.0015 (6) | 0.9048 (5) | 0.084 |
| OW(25) | 0.3283 (7) | 0.4004 (6) | 0.9399 (5) | 0.088 |
| OW (26) | 0.0316 (8) | 0.2083 (9) | 0.1395 (7) | 0.180 |
| $\mathrm{OW}(27) \dagger$ | 0.0000 | $0 \cdot 5000$ | $0 \cdot 0000$ | $0 \cdot 122$ |
| * Defined according to Hamilton (1959). <br> $\dagger$ Site occupation factor 0.5. |  |  |  |  |



Fig. 1. Arrangement of different V and O atom types in the decavanadate polyanion, according to Evans (1966).
(b) Distortions in the mmm symmetry arising from interactions with neighbouring atoms and groups. Table 3 shows the extreme and average values of the $\mathrm{V}-\mathrm{O}$ distances and $\mathrm{O}-\mathrm{V}-\mathrm{O}$ angles for each type of V and O atom. The ranges spanned by each type are a measure of the distortion from mmm symmetry. These distortions are similar to those reported for $\mathrm{K}_{2} \mathrm{Zn}_{2} \mathrm{~V}_{10} \mathrm{O}_{28}$.$16 \mathrm{H}_{2} \mathrm{O}$ (Evans, 1966) and correspond to deviations of no more than $0.04 \AA$ and $2^{\circ}$ from the distances and angles, respectively, reported by Evans. One of the more significant variations is observed in $\mathrm{V}(2)-\mathrm{O}(8)$ / $\mathrm{V}(2)-\mathrm{O}(9)\left(\mathrm{V}_{1}-\mathrm{O} d\right.$ type $)$ where a stronger hydrogen bond to $\mathrm{O}(8)$ lengthens $\mathrm{V}(2)-\mathrm{O}(8)$ by $0.031 \AA$ (Table 2) with respect to $V(2)-O(9)$, where $O(8)$ and $O(9)$ are related by the pseudomirror plane. This fact is supported by an $\mathrm{O}(8) \cdots \mathrm{O} W(16)$ distance of $2.662 \AA$ compared to $\mathrm{O}(9) \cdots \mathrm{O} W(27)=2.924 \AA$. Similar variations in interbond distances for $\mathrm{V}_{\mathrm{H}}-\mathrm{O} d, \mathrm{~V}_{11}-\mathrm{O} b$ and $\mathrm{V}_{\mathrm{I}}-\mathrm{O} b$ cannot be explained without the knowledge of the H positions due to the possibility of bifurcated and trifurcated hydrogen bonds (cf. Brink, 1971; Knop, Westerhaus \& Falk, 1980, and references therein).

Table 2. Interatomic distances $(\AA)$ and interbond angles $\left(^{\circ}\right.$ ) in the $\mathrm{VO}_{6}$ and $\mathrm{ErO}_{8}$ polyhedra (e.s.d.'s in parentheses)

|  | $\begin{aligned} & V_{1} \\ & V^{\prime}(1) \end{aligned}$ | $\begin{aligned} & \mathrm{Og} \\ & \mathrm{O}(1) \end{aligned}$ | $\begin{aligned} & \mathrm{O} d^{\prime} \\ & \mathrm{O}(2) \end{aligned}$ | $\begin{gathered} \mathrm{O} d \\ \mathrm{O}(3) \end{gathered}$ | $\begin{aligned} & \mathrm{O} b^{\prime} \\ & \mathrm{O}(4) \end{aligned}$ | $\begin{gathered} \mathrm{O} b \\ \mathrm{O}(5) \end{gathered}$ | $\begin{gathered} \mathrm{O} a \\ \mathrm{O}(6) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Og | $\mathrm{O}(1)$ | 1.617 (5) | $2 \cdot 696$ (7) | 2.710 (7) | $2.752(6)$ | 2.737 (5) | $3 \cdot 808$ (7) |
| $\mathrm{O} d^{\prime \prime}$ | $\mathrm{O}(2)$ | 103.2 (2) | 1.819 (4) | 2.719 (6) | $2 \cdot 702$ (6) | 3.761 (7) | $2 \cdot 645$ (5) |
| $\mathrm{O} d$ | $\mathrm{O}(3)$ | 103.9 (2) | 96.7 (2) | $1.821(5)$ | 3.771 (6) | 2.722 (6) | $2 \cdot 654$ (6) |
| $\mathrm{O} b^{\prime}$ | $\mathrm{O}(4)$ | 97.2 (2) | 88.9 (2) | $\overline{156.2(2)}$ | 2.032 (4) | 2.511 (5) | $2 \cdot 607$ (6) |
| $\mathrm{O} b$ | $\mathrm{O}(5)$ | 96.9 (2) | 156.6 (2) | 90.0 (2) | 76.6 (2) | 2.022(4) | $2 \cdot 632$ (7) |
| $\mathrm{O} a$ | $\mathrm{O}(6)$ | 171.6 (2) | 81.7 (2) | 82.0 (2) | 75.9 (2) | 77.0 (2) | $2 \cdot 200$ (5) |
|  | $\begin{aligned} & V_{t} \\ & V(2) \end{aligned}$ | $\begin{aligned} & \bigcirc b^{\prime} \\ & \mathrm{O}(4) \end{aligned}$ | $\begin{gathered} \mathrm{O} b \\ \mathrm{O}(5) \end{gathered}$ | $\begin{gathered} \mathrm{O} a \\ \mathrm{O}\left(6^{\prime}\right) \end{gathered}$ | $\begin{aligned} & \mathrm{Og} \\ & \mathrm{O}(7) \end{aligned}$ | $\begin{aligned} & \mathrm{O} d^{\prime} \\ & \mathrm{O}(8) \end{aligned}$ | $\begin{gathered} \mathrm{O} d \\ \mathrm{O}(9) \end{gathered}$ |
| $\mathrm{O} b^{\prime}$ | $\mathrm{O}(4)$ | 2.023 (4) | $2 \cdot 511$ (5) | $2 \cdot 613$ (7) | 2.780 (7) | 2.695 (6) | 3.740 (7) |
| $\mathrm{O} b$ | $\mathrm{O}(5)$ | 77.3 (2) | 1.998 (4) | $2 \cdot 618$ (7) | 2.769 (7) | 3.746 (6) | $2 \cdot 678$ (6) |
| $\mathrm{O} a$ | $\mathrm{O}\left(6^{\prime}\right)$ | 75.6 (2) | 76.3 (2) | $2 \cdot 230$ (5) | 3.838 (7) | $2 \cdot 660$ (6) | $2 \cdot 657$ (7) |
| Og | $\mathrm{O}(7)$ | 99.1 (2) | 99.6 (2) | 173.9 (2) | 1.613 (5) | 2.684 (6) | $2 \cdot 675$ (5) |
| $\mathrm{O} d^{\prime}$ | $\mathrm{O}(8)$ | 88.5 (2) | 155.6 (2) | 81.1 (2) | $102 \cdot 1(2)$ | 1.833 (4) | 2.706 (6) |
| Od | $\mathrm{O}(9)$ | 155.8 (2) | 89.5 (2) | 81.7(2) | $103 \cdot 0$ (2) | 96.2 (2) | 1.802 (4) |
|  | $\begin{aligned} & V_{11} \\ & V(3) \end{aligned}$ | $\begin{gathered} \mathrm{O} d \\ \mathrm{O}(2) \end{gathered}$ | $\begin{gathered} \mathrm{O} a \\ \mathrm{O}(6) \end{gathered}$ | $\begin{gathered} \mathrm{O} d \\ \mathrm{O}\left(9^{\prime}\right) \end{gathered}$ | $\begin{gathered} O f \\ O(10) \end{gathered}$ | $\begin{gathered} \mathrm{O} c \\ \mathrm{O}(11) \end{gathered}$ | $\begin{gathered} \mathrm{O} e \\ \mathrm{O}(12) \end{gathered}$ |
| Od | $\mathrm{O}(2)$ | 1.868 (5) | $2 \cdot 645$ (5) | 3.660 (6) | $2 \cdot 700$ (8) | 2.666 (7) | 2.603 (6) |
| $\mathrm{O} a$ | $\mathrm{O}(6)$ | 77.7 (2) | $2 \cdot 312$ (5) | $2 \cdot 657$ (6) | 3.920 (7) | 2.743 (6) | 2.658 (5) |
| $\mathrm{O} d$ | $\mathrm{O}\left(9^{\prime}\right)$ | 153.8 (2) | 77.7 (2) | 1.889 (4) | 2.727 (7) | 2.681 (7) | $2 \cdot 622$ (6) |
| Of | $\mathrm{O}(10)$ | 101.3 (2) | 172.4 (2) | $101.9(2)$ | 1.617 (4) | 2.730 (6) | 2.808 (7) |
| Oc | O(11) | 92.7 (2) | 82.4 (2) | 92.8 (2) | 105.2 (2) | $1.815(5)$ | $3 \cdot 813$ (6) |
| $\mathrm{O} e$ | $\mathrm{O}(12)$ | 82.3 (2) | 74.3 (1) | $82 \cdot 6$ (2) | 98.1(2) | $\overline{156.7(2)}$ | 2.079 (5) |
|  | $\begin{aligned} & V_{111} \\ & V_{(4)} \end{aligned}$ | $\begin{gathered} \mathrm{O} b \\ \mathrm{O}(4) \end{gathered}$ | $\begin{gathered} \mathrm{O} b^{\prime} \\ \mathrm{O}\left(5^{\prime}\right) \end{gathered}$ | $\begin{gathered} \mathrm{O} a \\ \mathrm{O}(6) \end{gathered}$ | $\begin{gathered} \mathrm{O} a^{\prime} \\ \mathrm{O}\left(6^{\prime}\right) \end{gathered}$ | $\begin{gathered} \mathrm{O} e \\ \mathrm{O}(12) \end{gathered}$ | $\begin{gathered} \mathrm{O} e^{\prime} \\ \mathrm{O}\left(13^{\prime}\right) \end{gathered}$ |
| $\mathrm{O} b$ | $\mathrm{O}(4)$ | 1.898 (4) | 3.752 (6) | $2 \cdot 607$ (5) | $2 \cdot 613$ (6) | 2.706 (7) | 2.709 (5) |
| $\mathrm{O} b^{\prime}$ | $\mathrm{O}\left(5^{\prime}\right)$ | 155.4(2) | 1.942 (5) | $2 \cdot 618$ (5) | $2 \cdot 632$ (7) | 2.720 (6) | $2 \cdot 678$ (7) |
| $\mathrm{O} a$ | $\mathrm{O}(6)$ | 80.9 (2) | 80.3 (2) | 2.113 (4) | $2 \cdot 650$ (8) | $2 \cdot 658$ (5) | 3.750 (7) |
| $\mathrm{O} a^{\prime}$ | $\mathrm{O}\left(6^{\prime}\right)$ | 80.3 (2) | 80.1 (2) | 77.0 (2) | 2.143(5) | 3.792 (6) | 2.661 (5) |
| $\mathrm{O} e$ | $\mathrm{O}(12)$ | 98.1 (2) | 97.1 (2) | 88.2 (2) | 165.2(2) | 1.681 (4) | 2.697 (7) |
| Oe ${ }^{\prime}$ | $\mathrm{O}\left(13^{\prime}\right)$ | 98.6 (2) | 95.3 (2) | 164.5 (2) | 87.6 (2) | 107.2 (2) | 1.671 (4) |
|  | $\begin{aligned} & V_{11} \\ & V^{\prime}(5) \end{aligned}$ | $\begin{gathered} \mathrm{Od} \\ \mathrm{O}(3) \end{gathered}$ | $\begin{gathered} \mathrm{O} a \\ \mathrm{O}(6) \end{gathered}$ | $\begin{gathered} \mathrm{O} d \\ \mathrm{O}\left(8^{\prime}\right) \end{gathered}$ | $\begin{gathered} \mathrm{O} c \\ \mathrm{O}(11) \end{gathered}$ | $\begin{gathered} \mathrm{O} e \\ \mathrm{O}(13) \end{gathered}$ | $\begin{gathered} O f \\ O(14) \end{gathered}$ |
| $\mathrm{O} d$ | $\mathrm{O}(3)$ | 1.878 (5) | $2 \cdot 654$ (6) | 3.632 (6) | 2.628 (7) | 2.586 (5) | 2.713 (7) |
| $\mathrm{O} a$ | $\mathrm{O}(6)$ | 77.0 (2) | 2.345 (4) | 2.660 (7) | 2.743 (6) | 2.661 (5) | 3.939 (7) |
| $\mathrm{O} d$ | $\mathrm{O}\left(8^{\prime}\right)$ | 154.3 (2) | 77.8 (2) | 1.847 (4) | 2.639 (6) | 2.650 (5) | 2.688 (7) |
| $\mathrm{O} c$ | $\mathrm{O}(11)$ | 89.6 (2) | 80.7 (2) | 91.1 (2) | 1.851 (4) | 3.793 (6) | 2.724 (6) |
| Oe | $\mathrm{O}(13)$ | 82.6 (2) | 74.5 (2) | 86.0 (2) | 155.0(2) | 2.034 (4) | 2.810 (6) |
| Of | O(14) | 102.4 (2) | $175 \cdot 2$ (2) | 102.4 (2) | 104.1 (2) | 100.7 (2) | 1.597 (5) |

Table 2 (cont.)

| Er | O(15) | $\mathrm{O}(16)$ | $\mathrm{O}(17)$ | $\mathrm{O}(18)$ | O(19) | $\mathrm{O}(20)$ | $\mathrm{O}\left(21^{\prime}\right)$ | $\mathrm{O}(22)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| O(15) | 2.375 (6) | 4.512 (6) | 2.800 (7) | 4.438 (7) | 3.085 (8) | 2.786 (8) | $2 \cdot 890$ (7) | 3.905 (8) |
| $\mathrm{O}(16)$ | 143.2 (2) | 2.380 (6) | 4.496 (7) | 2.881 (7) | 2.762 (7) | 2.975 (8) | $4 \cdot 149$ (7) | $2 \cdot 864$ (8) |
| $\mathrm{O}(17)$ | 71.8 (2) | 140.2(2) | 2.402 (5) | 2.989 (8) | 4.499 (8) | 3.991 (7) | 2.971 (7) | 2.808 (8) |
| $\mathrm{O}(18)$ | 140.5 (2) | $75 \cdot 2$ (2) | $78 \cdot 1$ (2) | 2.341 (5) | 3.841 (6) | 4.524 (7) | 2.824 (8) | 3.065 (6) |
| $\mathrm{O}(19)$ | 82.6 (2) | $72 \cdot 3$ (2) | $146 \cdot 2$ (2) | $111.7(2)$ | $2 \cdot 300$ (4) | 2.951 (5) | $2 \cdot 854$ (6) | 4.347 (7) |
| $\mathrm{O}(20)$ | 71.5 (2) | 77.1 (2) | 112.7 (2) | 145.8 (2) | 77.9 (2) | 2.391(5) | 4.466 (7) | 2.772 (8) |
| O(21') | 75.0 (2) | 121.7 (2) | 77.0 (2) | 73.6 (2) | 75.3 (2) | 139.3 (2) | $\underline{2.371(6)}$ | 4.482 (8) |
| $\mathrm{O}(22)$ | 111.9 (2) | 74.8 (2) | 72.7 (2) | 81.8 (2) | 139.2 (2) | 71.8 (2) | 144.2 (2) | $\underline{2.338(5)}$ |

Table 3. Average bond distances $\left(\AA^{\AA}\right)$ and angles $\left({ }^{\circ}\right)$ in the decavanadate ion

Numbers of averaged values are given in parentheses.

|  | Average | Range |
| :---: | :---: | :---: |
| $\mathrm{V}_{1}-\mathrm{Og}$ | 1.62 (2) | 1.613-1.617 |
| $\mathrm{V}_{1}-\mathrm{O} a$ | 2.22 (2) | 2.200-2.230 |
| $V_{1}-O b$ | 2.02 (4) | 1.998-2.032 |
| $\mathrm{V}_{1}-\mathrm{Od}$ | 1.82 (4) | 1.802-1.833 |
| $\mathrm{V}_{11}-\mathrm{Of}$ | 1.61 (2) | 1.597-1.617 |
| $\mathrm{V}_{\mathrm{H}}-\mathrm{O} a$ | 2.33 (2) | 2.312-2.345 |
| $\mathrm{V}_{\mathrm{II}}-\mathrm{Oc}$ | 1.83 (2) | 1.815-1.851 |
| $\mathrm{V}_{\mathrm{H}}-\mathrm{Od}$ | 1.87 (4) | 1.847-1.889 |
| $\mathrm{V}_{11}-\mathrm{Oe}$ | 2.06 (2) | 2.034-2.079 |
| $\mathrm{V}_{111}-\mathrm{Oe}$ | 1.68 (2) | 1.671-1.681 |
| $\mathrm{V}_{11}-\mathrm{O} a$ | 2.13 (2) | 2.113-2.143 |
| $\mathrm{V}_{11}-\mathrm{O} b$ | 1.92 (2) | 1.898-1.942 |
| $\mathrm{Og}-\mathrm{V}_{1}-\mathrm{Ob}$ | 98 (4) | 96.9-99.6 |
| $\mathrm{Og}-\mathrm{V}_{1}-\mathrm{Od}$ | 103 (4) | 102.1-103.9 |
| $\mathrm{O} a-\mathrm{V}_{1}-\mathrm{O} b$ | 76 (4) | 75.6-77.0 |
| $\mathrm{O} a-\mathrm{V}_{1}-\mathrm{O} d$ | 82 (4) | 81.1-82.0 |
| $\mathrm{O} b-\mathrm{V}_{1}-\mathrm{O} b^{\prime}$ | 77 (2) | 76.6-77.3 |
| $\mathrm{O} d-\mathrm{V}_{1}-\mathrm{O} d^{\prime}$ | 96 (2) | 96.2- 96.7 |
| $\mathrm{O} b-\mathrm{V}_{1}-\mathrm{O} d$ | 89 (4) | 88.5-90.0 |
| $\mathrm{O} b-\mathrm{V}_{1}-\mathrm{O} d^{\prime}$ | 156 (4) | 155.6-156.6 |
| $\mathrm{O} a-\mathrm{V}_{\mathrm{t}}-\mathrm{Og}$ | 173 (2) | 171.6-173.9 |
| $\mathrm{O} f-\mathrm{V}_{11}-\mathrm{O} e$ | 99 (2) | 98.1-100.7 |
| $\mathrm{Oa}-\mathrm{V}_{11}-\mathrm{Oe}$ | 74 (2) | 74.3-74.5 |
| $\mathrm{O} f-\mathrm{V}_{\mathrm{n}}-\mathrm{Oc}$ | 105 (2) | 104.1-105.2 |
| $\mathrm{O} f-\mathrm{V}_{11}-\mathrm{Od}$ | 102 (4) | 101.3-102.4 |
| $\mathrm{O} a-\mathrm{V}_{\mathrm{HI}}-\mathrm{O} c$ | 82 (2) | $80.7-82.4$ |
| $\mathrm{O} a-\mathrm{V}_{11}-\mathrm{O} d$ | 78 (4) | 77.0-77.8 |
| $\mathrm{Oc}-\mathrm{V}_{11}-\mathrm{Od}$ | 92 (4) | 89.6-92.8 |
| $\mathrm{O} d-\mathrm{V}_{11}-\mathrm{O} e$ | 83 (4) | 82.3-86.0 |
| $\mathrm{O} a-\mathrm{V}_{11}-\mathrm{Of}$ | 174 (2) | 172.4-175.2 |
| $\mathrm{O} c-\mathrm{V}_{11}-\mathrm{O} e$ | 156 (2) | 155.0-156.7 |
| $\mathrm{O} d-\mathrm{V}_{11}-\mathrm{O} d$ | 154 (2) | 153.8-154.3 |
| $\mathrm{O} e-\mathrm{V}_{111}-\mathrm{O} e^{\prime}$ | 107 (1) | 107.2 |
| $\mathrm{O} a-\mathrm{V}_{\mathrm{II}}-\mathrm{O} a^{\prime}$ | 77 (1) | 77.0 |
| $\mathrm{O} a-\mathrm{V}_{\mathrm{m}}-\mathrm{Oe}$ | 88 (2) | 87.6-88.2 |
| $\mathrm{O} a-\mathrm{V}_{11 \mathrm{I}}-\mathrm{O} b$ | 80 (4) | $80 \cdot 1-80 \cdot 9$ |
| $\mathrm{O} b-\mathrm{V}_{111}-\mathrm{O} e$ | 97 (4) | 95.3-98.6 |
| $\mathrm{O} b-\mathrm{V}_{\mathrm{HI}}-\mathrm{O} b^{\prime}$ | 155 (1) | 155.4 |
| $\mathrm{O} a-\mathrm{V}_{\mathrm{II}}-\mathrm{O} e^{\prime}$ | 165 (2) | 164.5-165.2 |

However, hydrogen bonding alone cannot explain the observed differences in interbond distances for the cases in which these forces are not operating, that is for $\mathrm{V}_{\text {III }}-\mathrm{Oe}$ type (very loosely hydrogen bonded) and for $\mathrm{V}_{\mathrm{III}}-\mathrm{O} a$ type (Oa type are not sterically accessible to a water molecule). Thus, at present there is no satisfactory explanation for the deviations from mmm symmetry.

The three ideal mean planes corresponding to the symmetry planes were calculated with a modified version of NRC22 (Ahmed \& Pippy, 1966), which includes the calculation of the standard deviation of the dihedral angles according to Ito (1981).* Dihedral angles between these planes are $89.86(1), 90 \cdot 30(1)$

[^2]

Fig. 2. Stereoscopic view of the structure down $\mathbf{a}^{*}$ with $\mathbf{b}^{*}$ horizontal.
and $90.11(1)^{\circ}$. $\chi^{2}$ values $\left[\chi^{2}=\sum(\Delta / \sigma)^{2}\right]$ for the three mean planes (77.7, 165.0 and 4.7 , respectively), indicate significant deviation from coplanarity in the two former cases. The $\chi^{2}$ value for the third plane would indicate true $m$ symmetry; however, the analysis of the distances to this plane of the assumed mirror-symmetry-related pairs of atoms indicates significant deviations from $m$ symmetry (i.e. the standard deviation is 0.02 against $0.008 \AA$ expected from experimental errors).

A stereoscopic projection of the unit cell down $\mathbf{a}^{*}$ is shown in Fig. 2. It can be seen that the structure is formed by layers of decavanadate ions and hydrated $\mathrm{Er}^{3+}$ ions parallel to ( 001 ), which are linked together by ionic forces and hydrogen bonds formed by interstitial and coordination water with O atoms in $\mathrm{V}_{10} \mathrm{O}_{28}^{6-}$. Intercalated layers of interstitial water molecules parallel to (001) are also clearly seen in the projection. Decavanadate groups and rare-earth polyhedra do not share coordination O atoms. The coordination polyhedron of $\mathrm{Er}^{3+}$ ions is a distorted square antiprism (Wells, 1975), with the $\mathrm{Er}-\mathrm{O}$ and $\mathrm{O}-\mathrm{O}$ distances given in Table 2.

In the last stages of refinement, a Fourier synthesis revealed the presence of an unexpected water molecule at a symmetry center. There are several reported structures in which the water molecules occupy site symmetries other than $C_{2 v}$ or its subgroups (cf. Guggenberger \& Sleight, 1969; Jensen, 1968; PierceButler, 1982). Librational rather than orientational disorder may be invoked to explain the existence of this 'centrosymmetric' water molecule, since it does not interact appreciably with neighboring groups, the
distances O -acceptor and the angles acceptor- O acceptor not being favorable for the formation of strong hydrogen bonds.

In a previous paper (Rigotti et al., 1981) we reported the crystalline structure for the complete series of rare-earth decavanadates and wrongly described erbium decavanadate (Group III) as a 24 -hydrate. It now seems reasonable to assume that structural differences between Groups III and IV are mainly due to the occupancy of a symmetry center by an interstitial water molecule, rather than by changes in the $\mathrm{Ln}^{3+}$ ionic radii, or any other inherent feature of the $\mathrm{Ln}^{3+}$ ions.

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## References

Ahmed, F. R. \& Pippy, M. E. (1966). NRC Crystallographic Programs for the IBM 360 system. NRC22, revised June 1970. Division of Pure Physics. National Research Council of Canada. Ottawa.

Baur, W. H. (1970). Trans. Am. Crystallogr. Assoc. 6. 129-155.
Brink, G. (1971). Spectrochim. Acta Parl A, 28. 1151-1155.
Brown. I. D. \& Shannon. R. D. (1973). Acla Cryst. A 29. 266-282.
Cromer, D. T. \& Mann. J. B. (1968). Acta Crist. A24. 321-324.
Debaerdemaeker. T.. Arrieta. J. M. \& Amigo. J. M. (1982). Acta Crist. B38. 2465-2468.
Durif. P. A.. Averbuch-Pouchot. M. T. \& Glittel., J. C. (1980). A cta Crist. B36, 680-682.
Evans. H. T. (1966). Inorg. Chem. 5. 967-977.
Guggenberger. L. J. \& Sielght. A. W. (1969). Inorg. Chem. 8. 2041-2046.
Hamilton. W. C. (1959). Acia Crist. 12, 609-610.
Ito. T. (1981). Acta Crist. A 37. 621-624.
Jensen. S. J. (1968). Acta Chem. Scaind. 22. 647-652.
K nop. O.. Westerhaus. W. J. \& Fal.k. M. (1980). Can. J. Chem. 58. 867-874.

Pierce-Butler, M. A. (1982). Acla Cryst. B38. 3097-3100.
Rigotti, G.. Punte, G.. Rinero. B. E.. Escobar. M. E. \& Baran. E. J. (1981). J. Inorg. Nucl. Chem. 43. 2811-2814.

Saf`ynov. Yu. N., Kuz'min. E. A. \& Belov. N. V. (1979). Kristallografịa, 24, 767-771.
Sheldrick, G. M. (1976). SHELX76. Program for crystal structure determination. Univ. of Cambridge. England.
Swallow. A. G.. Ahmed. F. R. \& Barnfs. W. H. (1966). Acia Crist. 21, 397-405.
Welis. A. F. (1975). Structural Inorganic Chemistry. 4th ed.. p. 64. Oxford: Clarendon Press.

# Structure of Monoclinic Rubidium Dideuteriumphosphate, $\mathrm{RbD}_{2} \mathbf{P O}_{4}$, in the Intermediate Phase 

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#### Abstract

M_{r}=184.44\), monoclinic, $P 2_{1} / c, \quad a=$ 7.683 (1), $\quad b=6 \cdot 170(1) . \quad c=9.560(1) \AA . \quad \beta=$ $109 \cdot 10(1)^{\circ}, \quad V=428.2 \AA^{3} . \quad Z=4, \quad D_{x}=$ $2.861 \mathrm{~g} \mathrm{~cm}^{-3}, \quad \lambda(\mathrm{CuK} \mathrm{\alpha})=1.54178 \AA, \quad \mu(\mathrm{Cu} K \alpha)=$ $202 \cdot 16 \mathrm{~cm}^{-1}, F(000)=344, T=332 \mathrm{~K}, R=0.040$ for 500 unique reflections. The intermediate phase has a superstructure of the basic $\mathrm{CsH}_{2} \mathrm{PO}_{4}$ type. The shape of the $\mathrm{PO}_{4}$ tetrahedron is rather regular. Two kinds of H atoms display extremely large thermal amplitudes of about $0.5 \AA . \mathrm{PO}_{4}$ tetrahedra are connected by these H atoms to form a zigzag chain running along $\mathbf{b}$.


Introduction. Monoclinic $\mathrm{RbD}_{2} \mathrm{PO}_{4}$ undergoes successive phase transitions at 377 and 317 K (Sumita.

Osaka \& Makita. 1981). It is known that the lowtemperature phase is ferrielectric and the intermediate and the high-temperature phases are paraelectric (Osaka. Sumita \& Makita. 1983). The crystal structure of the low-temperature phase was determined at room temperature by Makita. Sumita. Osaka \& Suzuki (1981). However. the structures of the other phases have not yet been determined. It is necessary to investigate the structures of these higher-temperature phases in order to clarify the mechanism of the successive phase transitions from the structural point of view. We now report the crystal structure of the intermediate phase. as part of a continuing study of the mechanism of the successive phase transitions.

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[^1]:    $\ddagger$ Lists of structure factors, anisotropic thermal parameters and least-squares-planes' data have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 39048 ( 25 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.
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[^2]:    * See deposition footnote.

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